

α, β, γ from charmless *B* decays

Summary of WG-4 contributions to San Diego CKM Workshop

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BABAR Wednesday meeting

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Outline

WG-4 sessions / themes:

conveners: M. Beneke, Y. Grossman, M. Hazumi, AH

- 1) $\sin(2\beta_{\text{eff}})$ from s-penguin decays
 -  determine $\Delta S = \sin(2\beta_{\text{eff}}) - \sin(2\beta_{\text{SM}})$ for the various modes
- 2) Extraction of α
 -  theory: isospin violation in $\pi\pi$, $\rho\pi$, $\rho\rho$
 -  experiment: isospin and Dalitz analyses
- 3) $B \rightarrow \pi\pi$, $K\pi$ decays
 -  discussion on theoretical and phenomenological interpretations
- 4) Theoretical methods
 -  QCD-improved and flavor-symmetry approaches
- 5) Other charmless decays
 -  $B \rightarrow VV$, $Q2B$
 -  charmless B decays at hadron machines

mainly discuss things we know less:
Belle's analyses, theory talks

BABAR speakers: please forgive !

$\sin(2\beta_{\text{eff}})$ from s-penguin decays

Experimental talks by

- Hara ($\phi K_S, \eta' K_S, f_0 K_S$): for all modes: Belle [275m] and BABAR[227m]

🖼️ “strange” first slide:

113 fb⁻¹ (SVD-1), 140 fb⁻¹ (SVD-2)

Belle: separate simple fits; use high S/N sample; easy to handle systematics

BABAR: single MV fit; use as many events as possible; checks of validity of PDFs and correlations between variables are important

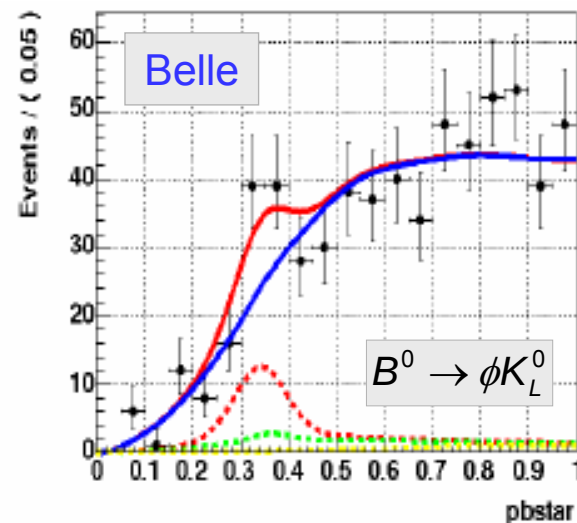
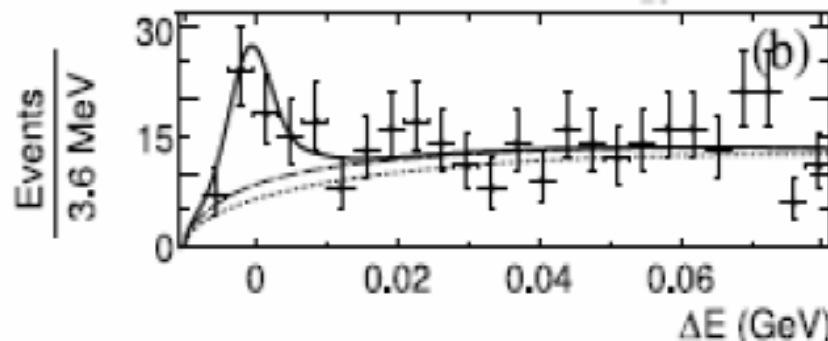
🖼️ continuum bkg: Belle L/ratio cut (P_B^* [cont] in ϕK_L from MC), BABAR: PDF in fit

🖼️ ϕK_S : **Belle :** use $\pi^+\pi^-$ ($N_S=139 \pm 14$) and $\pi^0\pi^0$ (13 ± 5)

BABAR : use $\pi^+\pi^-$ (114 ± 12)

🖼️ ϕK_L : **Belle :** ($N_S = 36 \pm 15$)

BABAR : (98 ± 18)



📖 B background : $K^+K^-K^0$ with opposite CP

Belle: obtained from sideband in ϕK^+ (find $6.7 \pm 1.2 \%$, but no f_0)

BABAR: from moments analysis $< 6.6 \%$ (@ 95% CL)

📖 other B bkg obtained from MC and fixed in fit, varied for systematics

most important in ϕK_L : $\phi K^{*0}(\rightarrow K_L \pi^0)$; take into account CP -even fraction ($\sim 24\%$)

📖 ML fit:

Belle: 2 vars in fit (CP)

BABAR: 35 parameters (CP , yields, PDF shapes)

📖 systematics (ϕK^0):

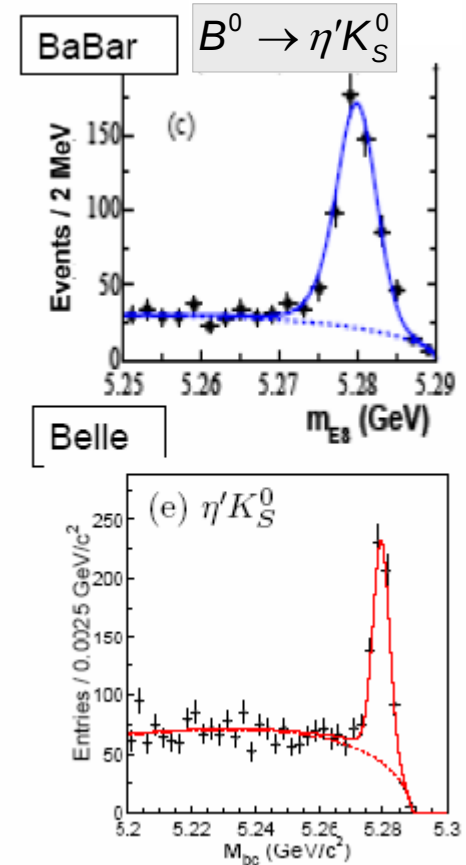
Belle: control samples ? resolution function; tag-side CPV: $\sigma(A) = 0.06$!; vertex: $\sigma(A) = 0.03$

📖 $\eta' K_S$: $\eta' \rightarrow \eta \pi^+ \pi^-$, $\rho^0 \gamma$ and $\eta \rightarrow \gamma \gamma$, $\pi^+ \pi^- \pi^0$ and $K_S \rightarrow \pi^+ \pi^-$
BABAR also: $\pi^0 \pi^0$

Belle: cont. fighting with L/ratio cut $\rightarrow N_S = 512 \pm 27$

BABAR: 804 ± 40

📖 fit strategy as in ϕK^0 : Belle floats CP parameters only, BABAR has 98 free parameters



systematics ($\eta'K_S$)

Belle: control samples ? resolution function; tag-side CP: $\sigma(A) = 0.03$!; vertex: $\sigma(A) = 0.03$

Big “?”: what type of MC fits is Belle doing ? Certainly toy; how about full MC ?

$f_0K_S : f_0 \rightarrow \pi^+\pi^-, K_S \rightarrow \pi^+\pi^-$

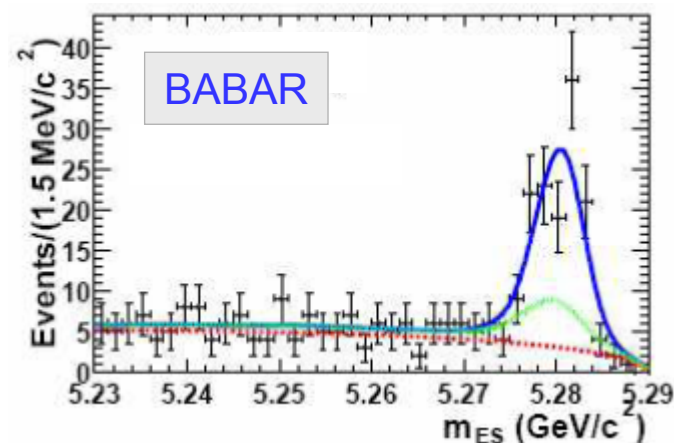
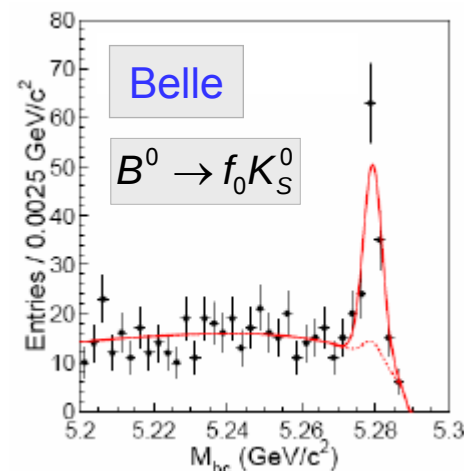
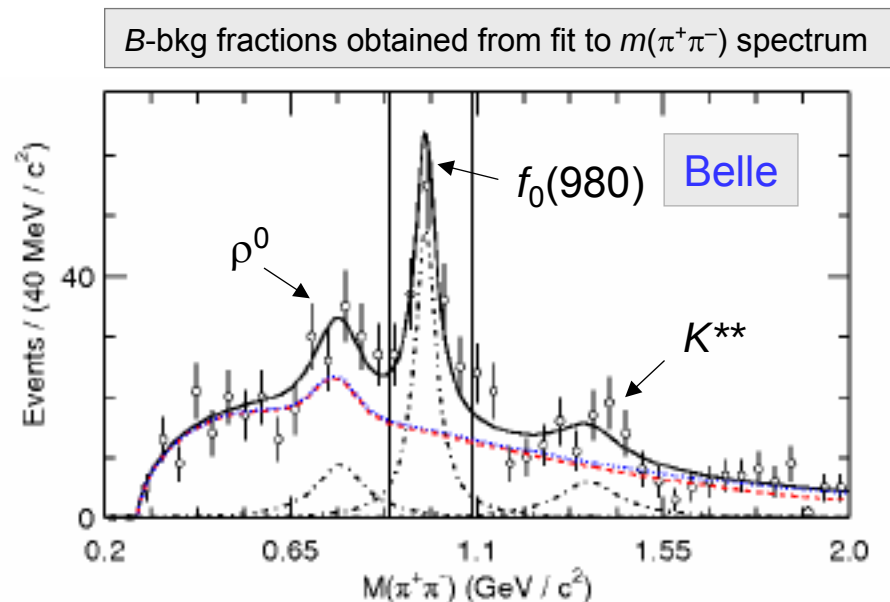
similar analysis/fit strategies as before

Belle: $N_S = 94 \pm 14$, 2 params. (CP); **BABAR:** 152 ± 19 , 41 params.

2.7σ difference on S between Belle and BABAR

systematics: similar; both account for Q2B approximation

BABAR: large syst. from fitting procedure!



- Wagner ($K^+K^-K_S$, $K_S K_S K_S$, $\pi^0 K_S$, ωK_S): for all modes: Belle [275m] and BABAR[227m]

$K^+K^-K_S$ (excluding ϕ)

similar analysis/fit strategies as before

Belle: $N_S = 399 \pm 28$, 2 params. (CP); BABAR: 452 ± 28 , 34 params.

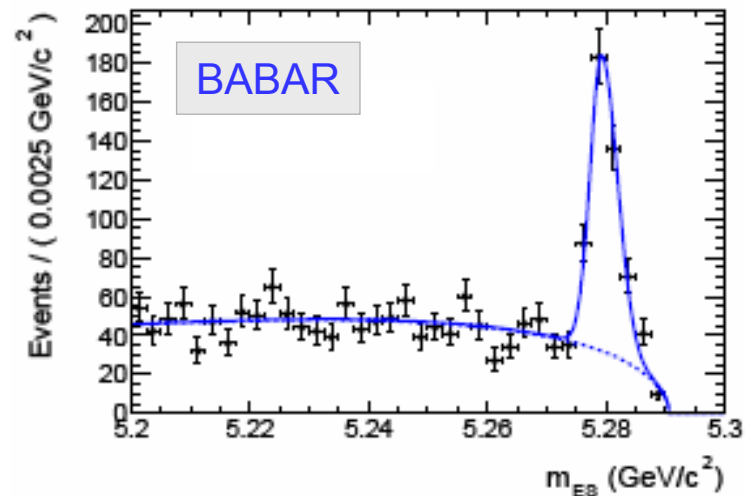
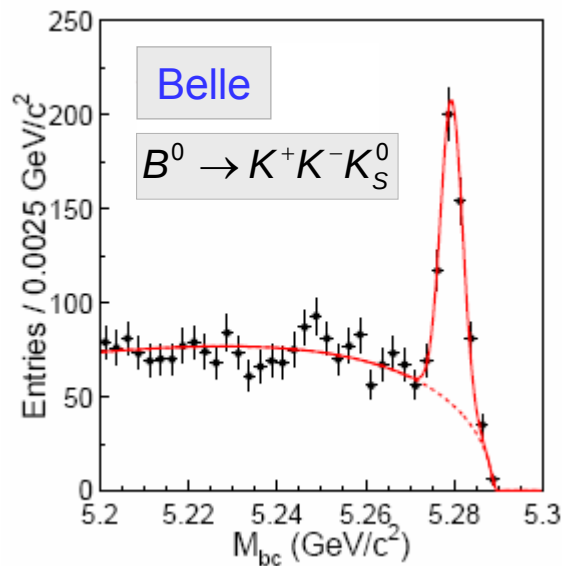
determination of CP-even fraction [$S = -(2f_{CP\text{-even}} - 1) \times \sin 2\beta$]

now (hep-ex/0504023):
 $0.83 \pm 0.10 \pm 0.04$

Belle: isospin relation: $f_{CP\text{-even}} = 2 \Gamma(B^+ \rightarrow K^+ K_S K_S) / \Gamma(B \rightarrow K^+ K^- K_S) = 1.03 \pm 0.15 \pm 0.05$

(neglects tree contributions and isospin violation from EW penguins)

BABAR: moments analysis: $f_{CP\text{-even}} = 0.89 \pm 0.08 \pm 0.06$ (the method of choice!)



🖥️ $\pi^0 K_S$:

🖥️ similar analysis/fit strategies as before

Belle: $N_S = 168 \pm 16$, 2 params. (CP); BABAR: 300 ± 23 , 34 params.

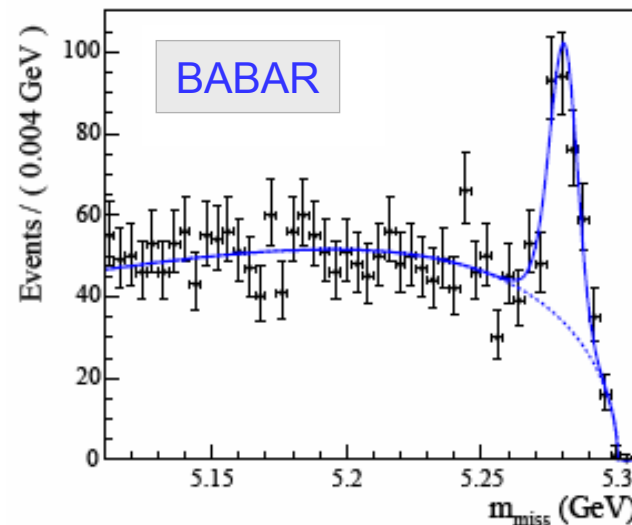
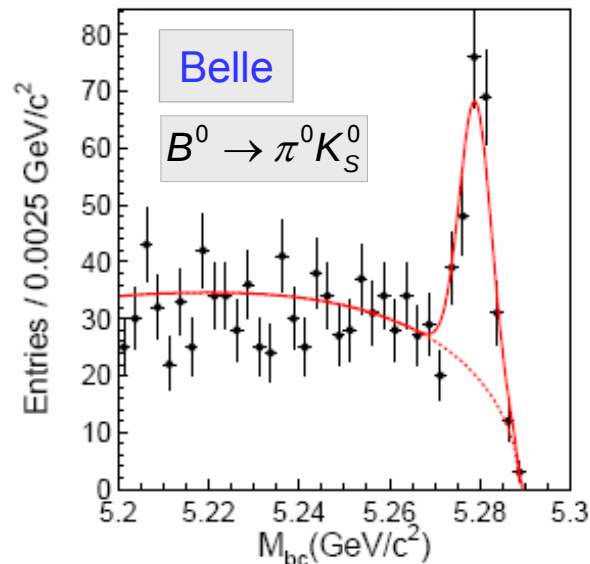
Belle loses large SVD-1 event fraction due to vertexing fiducial cuts

🖥️ both experiments use $J/\psi K_S$ events ignoring J/ψ tracks as CP control sample

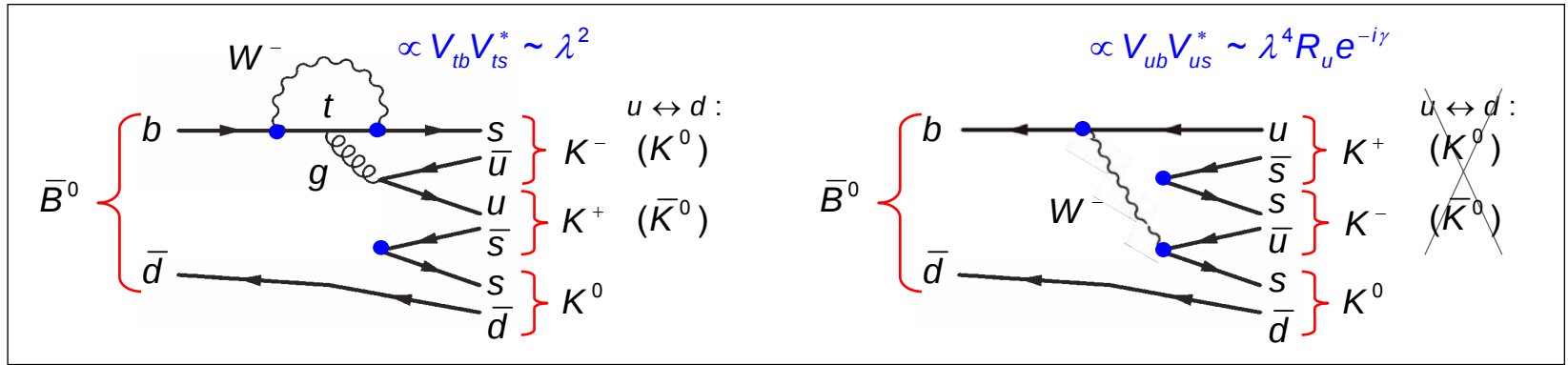
🖥️ systematics:

Belle: dominated by resolution function (0.05) and background fraction (0.07): sum is 0.11

BABAR: dominated by res fcn, CVT align., other B 's: sum is 0.04

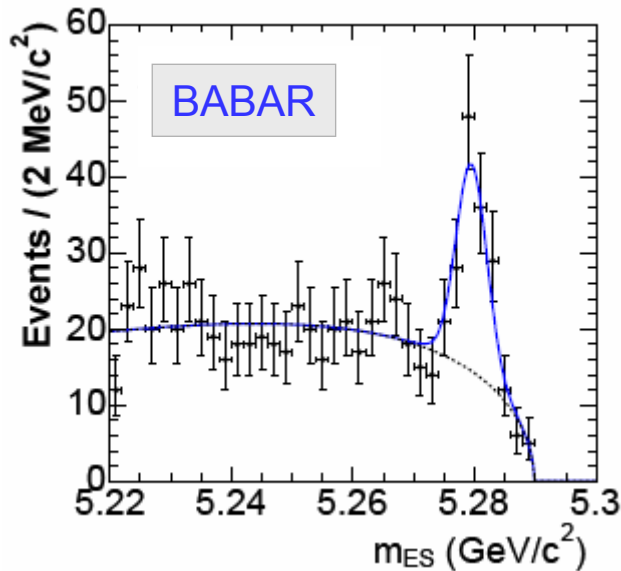
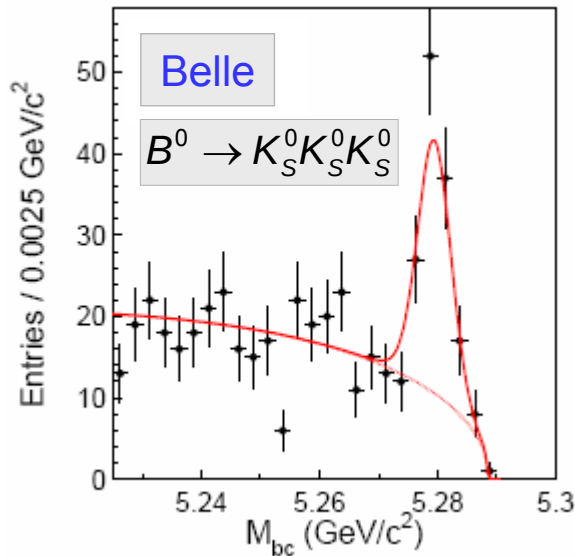


 $K_S K_S K_S$ (CP -even eigenstate, new golden mode)



 Belle also allows one $K_S \rightarrow \pi^0 \pi^0$

Belle: $N_S[\text{tot}] = 88 \pm 13$ [16 ± 8 $K_S \rightarrow \pi^0 \pi^0$] (CP measurement); BABAR: 88 ± 10 (CP and BR)



both experiments exclude $(\chi_{c0}, D^0) \rightarrow K_S K_S$ events

2.5 σ difference on S between Belle and BABAR

Statistical error factor 1.9 better for BABAR

Large systematic error on S for Belle: 0.20 (resolution fcn and bkg); BABAR: 0.04

🖥️ ωK_S (new s-penguin mode; possibly somewhat larger tree pollution than other modes → see later)

🖥️ similar analysis/fit strategies as before

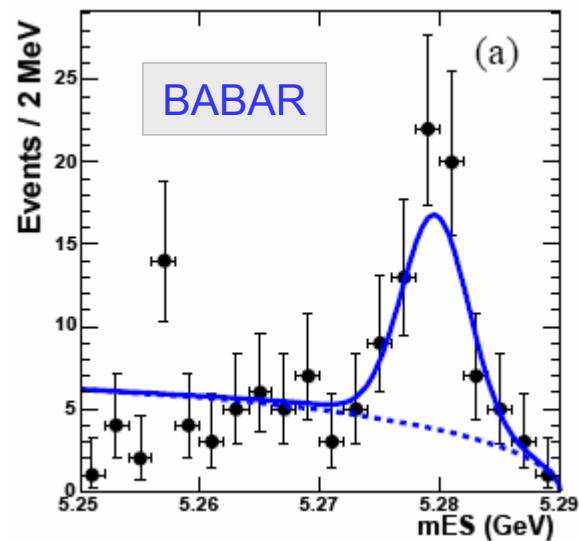
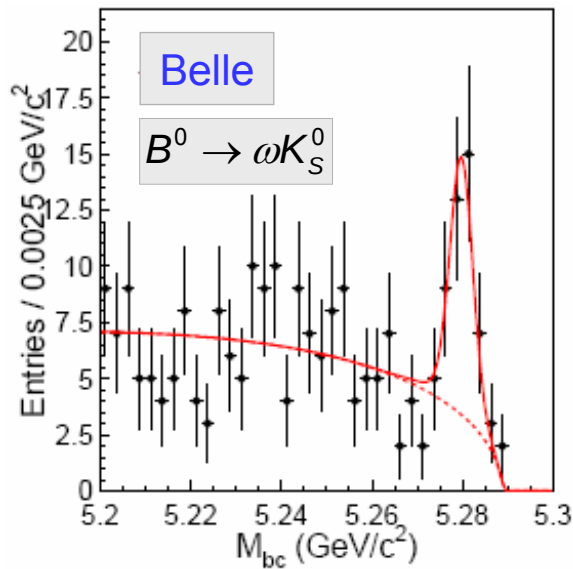
Belle: $N_S = 31 \pm 7$; BABAR: 96 ± 14

BABAR more than 3 times more signal events with less data → analysis strategy !!

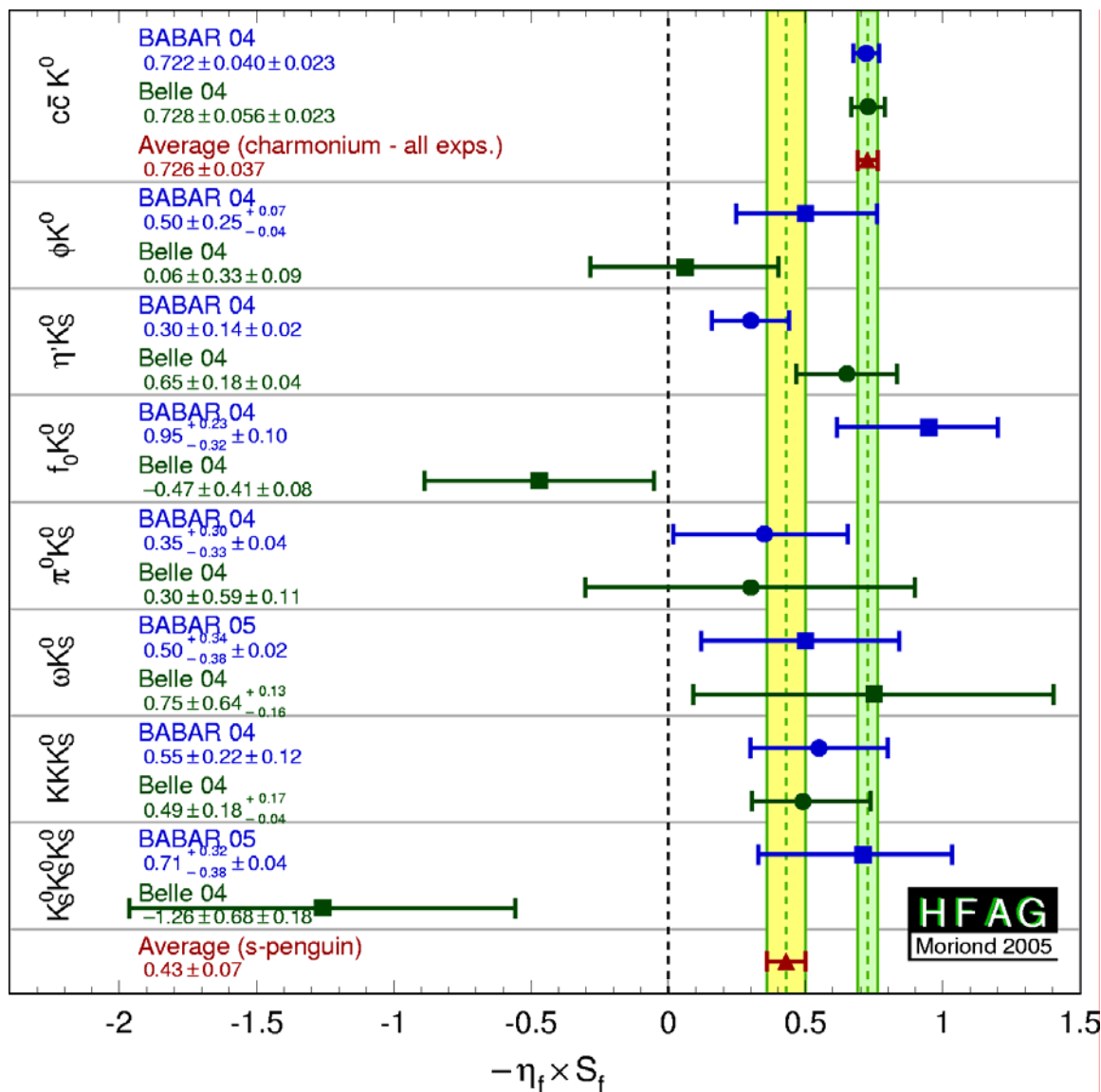
🖥️ systematics:

Belle: ~ 0.15 (dominated by bkg, fit bias (!) and resolution fcn)

BABAR: 0.04



$\sin(2\beta_{\text{eff}})$ from s-penguin decays: experimental summary



no indication
for direct CPV

Theory: $\Delta S \equiv \sin(2\beta_{\text{eff}}) - \sin(2\beta)$

- Most urgent theoretical question: determine ΔS for the various s-penguin modes

approaches: SU(3) flavor symmetry (Ligeti)

QCD-improved (Beneke, Pierini)

- Ligeti:

Grossman-Ligeti-Nir-Quinn, hep-ph/0303171

also discusses: CKM phase from eff. tree processes (same ρ - η point as in standard CKM fit)

photon polarization in $B \rightarrow X \gamma$: concludes that $S(f_s \gamma) \sim O(0.1)$ possible (RH photons)

SU(3) analysis: recalls that estimates are not optimal, and theory errors not statistical

$$A(\underbrace{B^0 \rightarrow f_s}_{b \rightarrow q \bar{q} s}) = \underbrace{V_{cb}^* V_{cs}}_{[\lambda^2]} a_{f_s}^c + \underbrace{V_{ub}^* V_{us}}_{[\lambda^4]} a_{f_s}^u = V_{cb}^* V_{cs} a_{f_s}^c (1 + \xi_{f_s})$$

naïve: $\xi_f \sim O(0.03)$

$$A(\underbrace{B^0 \rightarrow f_d}_{b \rightarrow q \bar{q} d}) = \underbrace{V_{cb}^* V_{cd}}_{[\lambda^3]} b_{f_d}^c + \underbrace{V_{ub}^* V_{ud}}_{[\lambda^3]} b_{f_d}^u = V_{ub}^* V_{ud} b_{f_d}^u (1 + \lambda^2 \xi_{f_d}^{-1})$$

more sensitive to ξ_f

SU(3) relates a_{f_s} to b_{f_d} : $a_f^u = \sum_{f_d} x_{f_d} b_{f_d}^u$

Branching ratios constrain

$$\left| \frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cs}} \frac{b_{f_d}^u}{a_{f_s}^c} \right| \sim \sqrt{\frac{B(f_d)}{B(f_s)}}$$

Combine SU(3) and data for conservative upper limit:

$$|\xi_{f_s}| = \left| \frac{V_{ub}^* V_{us}}{V_{cb}^* V_{cs}} \frac{a_{f_s}^u}{a_{f_s}^c} \right| < \lambda \sum_{f_d} |x_{f_d}| \sqrt{\frac{B(f_d)}{B(f_s)}}$$

numerical results (limits at 90% CL)

$$\left| \xi_{\eta' K^0} \right| < 0.17 \quad (< 0.08 \text{ with } \eta' K^+ \text{ assuming equal trees, and } m_d = m_s)$$

$$\left| \xi_{\phi K^+} \right| < 0.23 \quad (\text{assumptions as above})$$

Denis D. and I found (using CKMfitter for proper error propagation):

(see Denis' talk at: http://www.slac.stanford.edu/BFROOT/www/Physics/WednesdayMeetings/W020205/sin2b-penguin_Uncertainty.pdf)

$$\left| \xi_{\eta' K^0} \right| < 0.14 \quad (< 0.07 \text{ with } \eta' K^+ \text{ assuming equal trees, and } m_d = m_s)$$

(< 0.10 simplified - ignoring some suppressed modes)

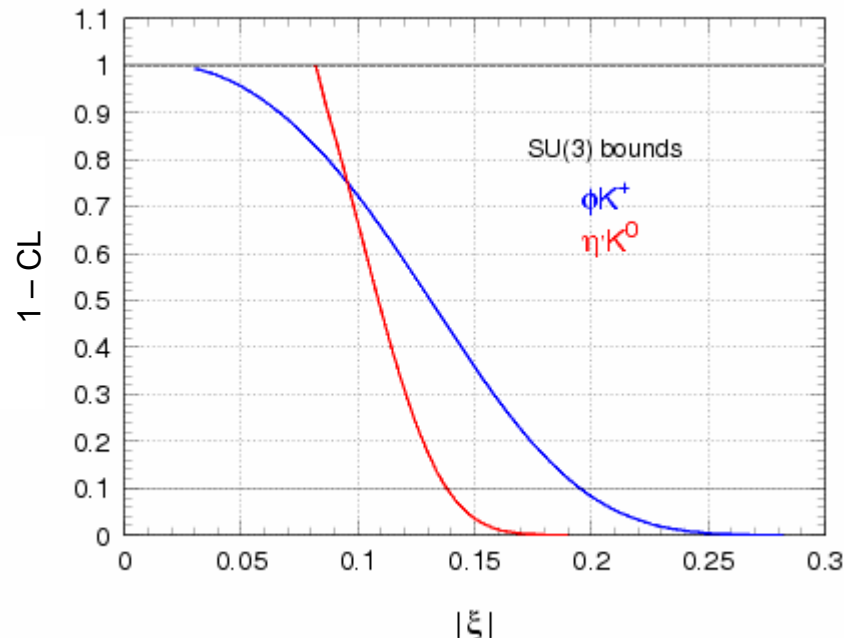
$$\left| \xi_{\phi K^+} \right| < 0.19$$

also limits on

$$\left| \xi_{K^+ K^- K_S} \right| < 0.19$$

$$\left| \xi_{\pi^0 K_S} \right| < 0.15$$

measurement of $K^* K^0$ (and others) required



■ Beneke:

Beneke-Neubert, hep-ph/0308039

🖥️ nicely responded to the Q's from the workshop

🖥️ discusses all modes, but $f_0 K^0$ (unclear quark content) and KKK^0 (3-body modes, no theory)

🖥️ ansatz:

$$A(\bar{B}^0 \rightarrow f) = \underbrace{V_{cb}^* V_{cs}}_{[\lambda^2]} a_{f_s}^c + \underbrace{V_{ub}^* V_{us}}_{[\lambda^4]} a_{f_s}^u \propto 1 + e^{-i\gamma} d_f$$

$$\Delta S \propto \text{Re}(d_f) \underbrace{\cos(2\beta) \sin \gamma}_{\sim 0.6} \quad \text{and} \quad C \propto \text{Im}(d_f) \underbrace{\sin \gamma}_{0.9}$$

➡ if d_f is small: S_f and C_f involve independent hadronic parameters

Remarks:

- final state rescattering included
- uncertainties: form factors, power corrections, weak annihilation, light-cone fcn's, ...
- hierarchies (in relevance for s-penguin modes) for topological amplitudes
 - *rather certain*: T irrelevant, P_{EW} contribute
 - *less certain*: $P^{c,u}$ for PP very important, $P_{EW,C}$ negligible
 - *uncertain*: $P^{c,u}$ for PV+VP very important, C important, $S^{c,u}$ contribute

pattern, neglecting unimportant modes:

of order one, corrected for CKM suppression

$$\begin{array}{ll}
 \pi K_S & \hat{d}_f \sim \frac{[-P^u] + [C]}{[-P^c]} \\
 \eta' K_S & \hat{d}_f \sim \frac{[-P^u] - [C]}{[-P^c]} \\
 \eta K_S & \hat{d}_f \sim \frac{[P^u] + [C]}{[P^c]} \\
 \rho K_S & \hat{d}_f \sim \frac{[P^u] - [C]}{[P^c]} \\
 \phi K_S & \hat{d}_f \sim \frac{[-P^u]}{[-P^c]} \\
 \omega K_S & \hat{d}_f \sim \frac{[P^u] + [C]}{[P^c]}
 \end{array}$$

[Quantities in square brackets have positive real part.]

$|P^u/P^c|$ are roughly independent of f but (magnitude of real parts)

$$P^c(\pi K) \sim 2P^c(\rho K) \sim 0.4P^c(\eta' K) \sim 2.3P^c(\eta K) \sim 1.3P^c(\phi K) \sim 2.3P^c(\omega K)$$

hence the influence of C determines the difference between the different modes.

results:



Mode	Theory $\delta \sin(2\beta)_f$	[Range]*	Experiment
πK_S	$0.07^{+0.05}_{-0.04}$	[+0.02, 0.13]	$-0.39^{+0.27}_{-0.29}$
ρK_S	$-0.08^{+0.08}_{-0.12}$	[-0.24, 0.02]	—
$\eta' K_S$	$0.01^{+0.01}_{-0.01}$	[-0.01, 0.03]	-0.32 ± 0.11
ηK_S	$0.10^{+0.11}_{-0.07}$	[-1.45, 0.27]	—
ϕK_S	$0.02^{+0.01}_{-0.01}$	[+0.01, 0.04]	-0.39 ± 0.20
ωK_S	$0.13^{+0.08}_{-0.08}$	[+0.03, 0.19]	$0.02 \pm 0.64^{+0.13}_{-0.16}$

* range determined with scans requiring the exp. BRs to be within 3σ

🖥️ discussion points:

- expected deviations mostly positive !
- very small uncertainties for $\eta'K_S$ and ϕK_S
- direct CP measurement of no use, if it is small
- **SU(3) is of no use: n - n' and ω - ϕ mixing are $O(1)$ effects**
→ roughly, the argument goes like: QCDF is $O(\Lambda_{\text{QCD}}/m_b \sim 0.1)$, while SU(3) is $O(0.3)$

🖥️ how to obtain large ΔS ? [recall: $\text{Re}(d_f) \sim \varepsilon_{\text{CKM}} \times \text{Re}(a^u / a^c)$]

- suppression of a^c ? cancellation between amplitudes excluded by BR measurements
- enhancement of a^u ? needs to be several times larger than predicted by QCDF... not possible
- if to be explained by hadronic effects, possibly large enhancement of u -penguin

my comment: note that this scenario is favored
by current $\pi\pi$, $K\pi$ data

🖥 introductory remarks:

- a clear demonstration that penguins *do* factorize is still missing
 - Λ_{QCD}/m_b corrections may be important

🖥 charming penguin approach:

- take tree $E_{1,2}$ and pert. LO contributions from QCDF
 - parameterize (RGI)q P^c , P^{c-u} , annihilation by complex amplitudes (neglect OZI-suppr. terms)

fit for these using data

🖥 ansatz: $\sqrt{2} \cdot A(B^0 \rightarrow K^0 \pi^0) = \underbrace{-V_{tb}^* V_{ts}}_{[\lambda^2]} P(c) - \underbrace{V_{ub}^* V_{us}}_{[\lambda^4]} (E_2 + P_1^{\text{GIM}}(u - c))$

🖥 what about EW penguins ? Neglected ?

🖥 results for fits to all isospin-related modes:

$$\begin{aligned} \Delta S(\pi^0 K^0) &= + 0.04 \pm 0.02, \text{ no/small direct CPV} \\ \Delta S(\pi^0 K^{*0}) &= + 0.05 \pm 0.06, \text{ no/small direct CPV} \\ \Delta S(\rho^0 K^0) &= - 0.02 \pm 0.05, \text{ no/small direct CPV} \\ \Delta S(\phi^0 K^0) &= + 0.03 \pm 0.05, \text{ no/small direct CPV} \end{aligned}$$

s-penguins: my personal conclusions

- “QCD-improved” authors agree quantitatively (also on the sign of ΔS)
- only data-driven fits are predictive when $\Delta S \sim O(0.1)$
- for $\eta' K^0$ and ϕK^0 $\Delta S \sim O(0.01) \rightarrow$ even large errors in the theory would not lead to large ΔS
- why would SU(3) be better than Factorization ?
(only because it produces worse bounds, doesn't make it more reliable ;-))
- what if u -penguins are huge ? ... and why would that be ?

Extraction of α

Experimental talks by

- Ishino ($B \rightarrow \pi\pi$) [nice talk!] : Belle [275m] and BABAR[227m] for $\pi^+\pi^-$

 continuum suppression :

- Belle uses Super-FW moments: these involve the final B_{CP} state momenta, and hence are different for each final state: how to validate these with BReco events ? Never saw a validation plot !
- Belle: L/ratio cut; BABAR: Fisher in fit

 Fit yields :

- Belle: $N_{\pi\pi} = 666 \pm 43$, $N_{K\pi} = 247 \pm 31$ (after PID cut); 2 parameter fit (2820 events in fit)
- BABAR: $N_{\pi\pi} = 467 \pm 33$, $N_{K\pi} = 1606 \pm 51$; 46 parameter fit (two-step fit ☹)

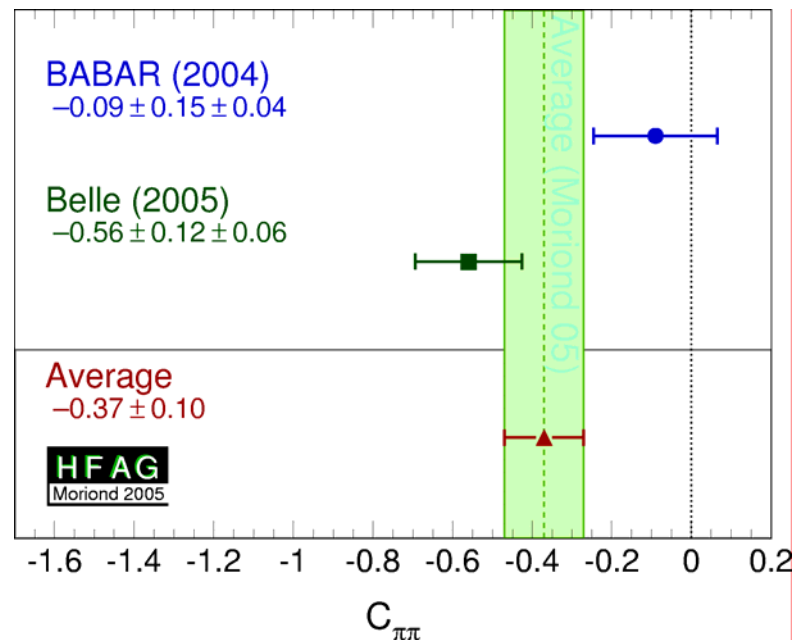
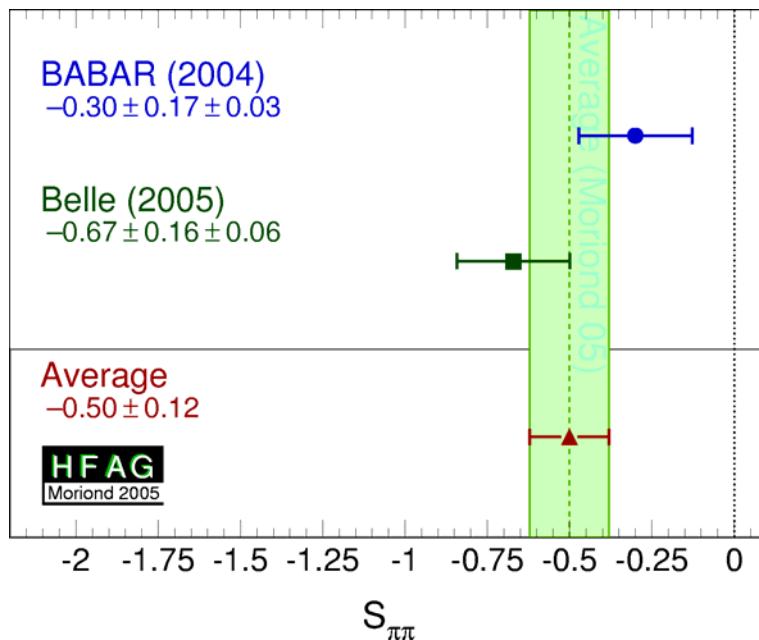
 Validations :

- both: tag-cat dependent S & B PDFs; τ_B and Δm_d measurements; similar systematics
- Belle: $\Delta t(\text{cont})$ obtained from sideband events
cont CP asymmetries varied for systematics
full MC fits ?
no likelihood ratio plot and/or sPlots;
fits for subsets with different S/N ... consistency within stat. errors



Results :

S & C combined: 3.2 (ICHEP'04) $\rightarrow$ 2.3 σ discrepancy



Belle's direct CPV check:
 (time-integrated fit)

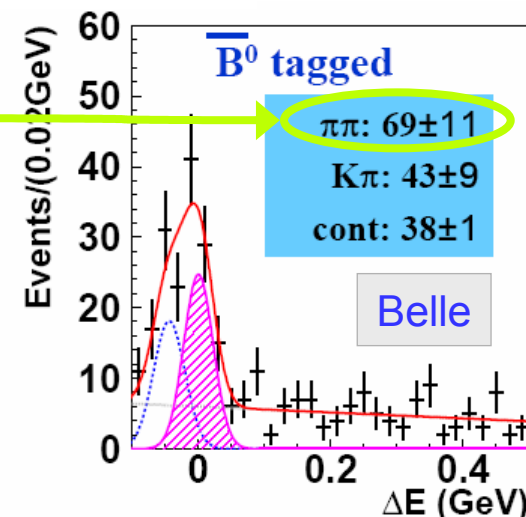
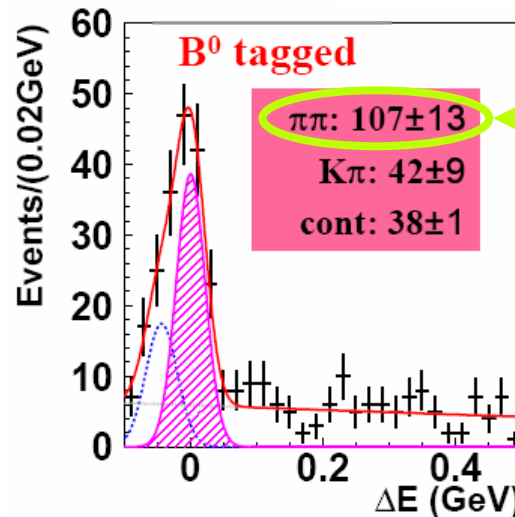


amusing SU(3) trick:

$$A_{CP}(K^+\pi^-) = -0.11 \pm 0.02 \rightarrow \approx \text{SU}(3)$$

$$\frac{1}{3}C(\pi^+\pi^-) = -0.12 \pm 0.03 \rightarrow$$

Gronau-Rosner, hep-ph/0405173



■ Bevan ($B \rightarrow \rho\rho$) BABAR[227m] for $\rho^+\rho^-$ and $\rho^0\rho^0$ – nothing from Belle yet ☹

🖥 introduction to isospin analysis and complication with CPV in $B \rightarrow VV$ decays

🖥 presentation of $B^0 \rightarrow \rho^0\rho^0$ measurement, and effect on isospin analysis

🖥 presentation of $B^0 \rightarrow \rho^0\rho^0$ pointing out improvements (mainly B -bkg treatment)

■ very nice summary of complicated analysis

■ discussion of interference effects with $\rho\pi\pi$ and $a_1\pi$

🖥 Isospin analysis predicts that $B^+ \rightarrow \rho^+\rho^0$ is somewhat large

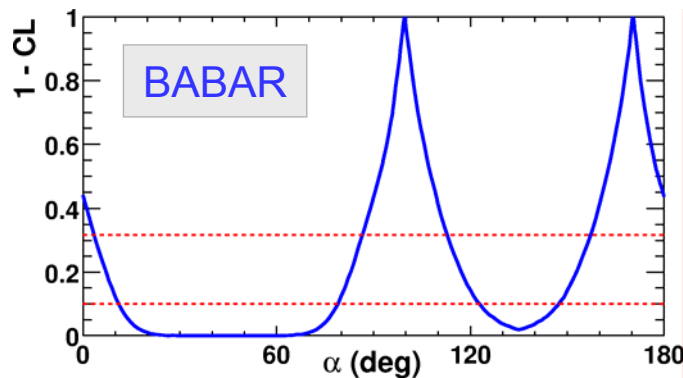
■ Belle [93m]: $B(\rho^+\rho^0) = 31.7 \pm 7.1^{+3.8}_{-6.7}$

■ BABAR [89m]: $B(\rho^+\rho^0) = 22.5^{+5.7}_{-5.4} \pm 5.8$

} are the large B backgrounds correctly subtracted ?

🖥 New toy-based frequentist determination of α :

■ BABAR and Belle use same (or similar) method for isospin analysis: easy to average



$\alpha_{\text{[SM]}} = (100 \pm 13)^\circ$ with 11° due to penguins

■ Graham ($B \rightarrow \rho\pi$) BABAR[213m] for full DP analysis

📖 introduction to phenomenological framework, isospin analysis (pentagon)

📖 Q2B analysis (only ρ bands on DP): Belle [152m]

- similar as other charmless analyses
- tight cut on ρ helicity angle: $|\cos\theta| > 0.5$ to fight cont
- $E(\pi^0)$ dependent ΔE and m_{bc} (like us)
- distinguish correct and wrong charge
- 3 B -bkg components: ρK , generic BB and rare B
- $N_S = 483 \pm 46$ (BABAR[213m]: 1184 ± 58 , full Dalitz)

📖 difficulties for Q2B analysis: needs super- B statistics

📖 direct CPV: BABAR dominates and Belle agrees

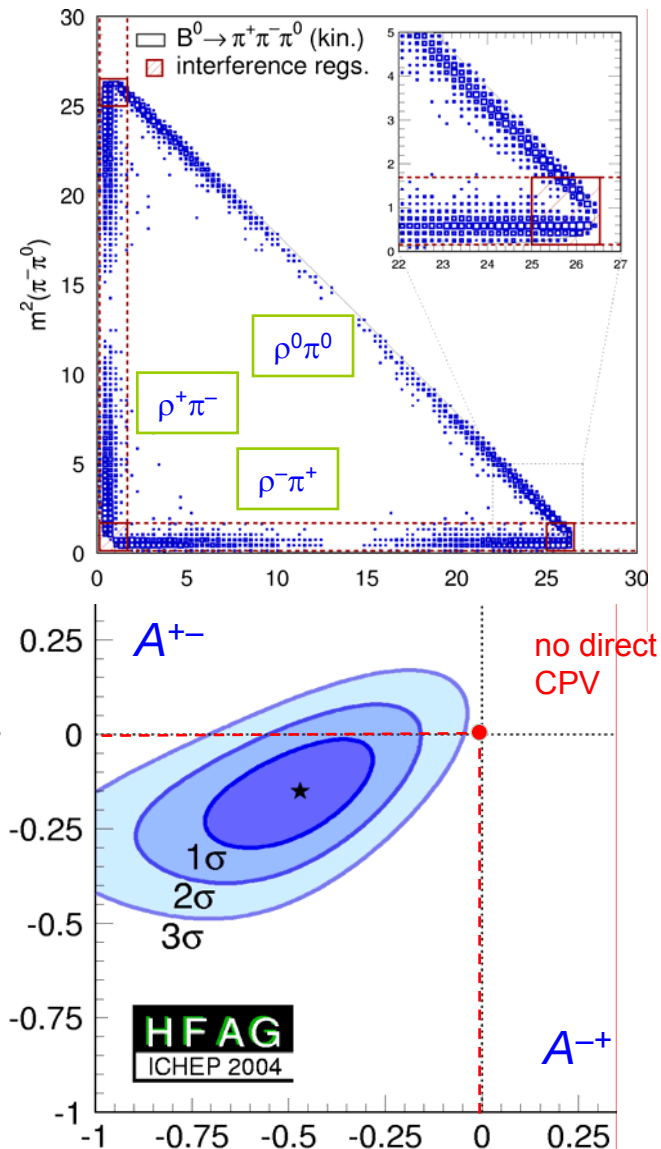
- QCDF predicts small penguins: very small direct CPV !

Average : BABAR (213m) & Belle (152m)			
A^{+-}	-0.15 ± 0.09	A^{-+}	$-0.47^{+0.13}_{-0.14}$

$$\Delta\chi^2(\text{no direct CPV}) = 14.5 \text{ (CL} = 0.00070 \Rightarrow 3.4\sigma\text{)}$$

📖 presentation of Dalitz plot analysis with 27 obs., etc

- see $\rho^0\pi^0$, but do not confirm large BR from Belle !



Theory talks by

- Buchalla ($B^0 \rightarrow \pi^+\pi^-, \rho^+\pi^-, \rho^+\rho^-$)

Buchalla-Safir, hep-ph/0406016

similar idea in Gronau et al.,
hep-ph/0410170

🖥 bounds on η from CP measurements only, ignoring $SU(2)$ partners:

- assuming strong phase $< |90^\circ|$
- use as input $\sin(2\beta)$

🖥 hmhhh ...

- Zupan (isospin violation in $B \rightarrow \pi\pi, \rho\pi, \rho\rho$) [nice talk!]

Gronau-Zupan, hep-ph/0502139

🖥 isospin breaking:

- source are d, u charges different, quark-mass differences
- typical size: $(m_u - m_d)/\Lambda_{\text{QCD}} \sim 1\%$
- extend basis of operators to $P_{\text{EW}}: Q_{7,\dots,10}$
- mass eigenstate $\neq$ isospin eigenstates $\rightarrow$ mixing (π^0 - η - η' , ρ - ω)
- may induce $\Delta I = 5/2$ transitions

🖥 EW penguins:

- can be Fierz-related to $\Delta I = 3/2$ (tree) amplitude: $e^{i\gamma} A^{+0} = e^{-i(\gamma+2\delta)} \bar{A}^{+0}$, with $\delta \approx 1.5^\circ$
- neglects $Q_{7,8}$
- also holds for $\rho\pi, \rho\rho$

π^0 - η - η' mixing :

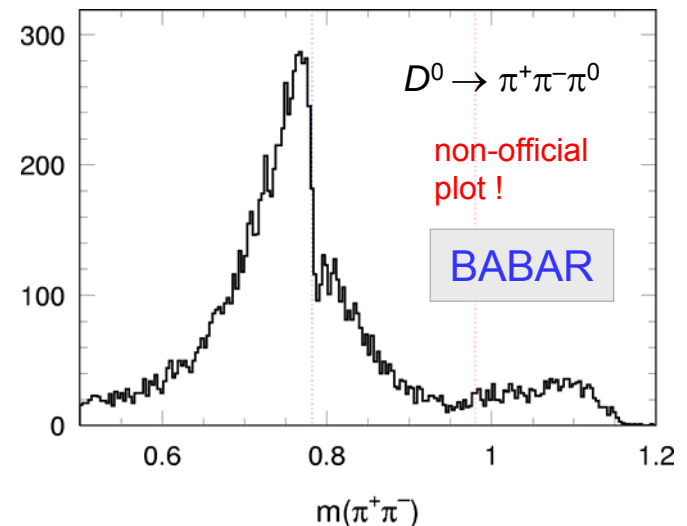
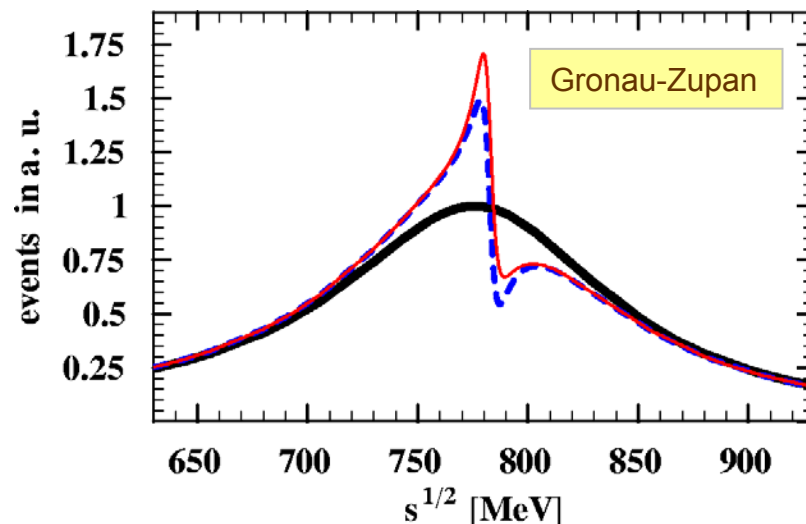
- $|\pi^0\rangle = |\pi_3\rangle + \varepsilon|\eta\rangle + \varepsilon'|\eta'\rangle$, with known $\varepsilon, \varepsilon'$
- would create direct CPV in $\pi^+\pi^0$
- bound from SU(3): $\Delta\alpha < 1.4^\circ$; much smaller bound ($< 0.1^\circ$) for $\rho\pi$

$B \rightarrow \rho\rho$

- $\Gamma_\rho > 0 \rightarrow \Delta I = 1$ contributions possible (like in $\rho\pi$)
- $O(m_\rho / \Gamma_\rho)^2$ effect; can be reduced experimentally by tighter m_ρ cuts

ρ - ω mixing : must be there ! (also for $B \rightarrow \rho\pi$)

- determined from fits to $\pi^+\pi^-$ spectrum
- expect large effect, since: $|A(B^+ \rightarrow \rho^+\omega) / A(B^+ \rightarrow \rho^+\rho^0)| = 0.69 \pm 0.41$
- however: integrated effect is small ($< 2\%$)



$B \rightarrow \pi\pi, K\pi$ decays

Experimental talks by

- Cristinziani (BRs and A_{CP} in $B \rightarrow \pi\pi, K\pi$) : Belle [275m] and BABAR[227m] for $\pi^+\pi^-$

 analysis status :

- Belle: BRs mostly (but $\pi^0\pi^0$) with 85m BB , A_{CP} with 275m
- BABAR: most with 227m, but $BR(h^+h^-)$

 strategies similar as in previous CP analyses

- I would love to see sPlots from Belle !

 radiative corrections are major issue for BR measurements

- copious 2-body BRs are now systematically limited

 results:

- no evidence for $B^0 \rightarrow K^+K^-$ (need combined limit for phenom. analyses)
- ~ agreement for $\pi^0\pi^0$ signal (Belle: 82 ± 16 , BABAR: 61 ± 17 (twice smaller BR))
- large $BR(K^0\pi^0)$ confirmed
- no $K_S K_S$ signal seen by Belle (BABAR has 4.5σ evidence)
- approximate Lipkin sum rule (relating A_{CP} and BRs between $K\pi$ modes) satisfied

 future of $\pi\pi$ isospin analysis is entirely driven by $\pi^0\pi^0$ mode !

Theory of $B \rightarrow \pi\pi, K\pi$ decays

■ Buras (introduction)

🖼 confront 16(−1) $\pi\pi, K\pi$ observables with theory/flavor symmetry

🖼 weak effective Hamiltonian: $H_{\text{eff}} = \frac{G_F}{\sqrt{2}} \sum_{i=1\dots 10} C_i(\mu) Q_i$

- C_i are short-distance Wilson coefficients, mostly known to NNLO pQCD
- Q_i are long-distance local tree, QCD penguin and EW penguin operators: unknown

🖼 theoretical strategies:

- diagrammatic approach and SU(3)-flavor (problem: no explicit relation with H_{eff})
- calculations of the matrix elements (QCDF, pQCD, SCET, ...)
- admixtures between these

🖼 $B \rightarrow \pi K$ decays:

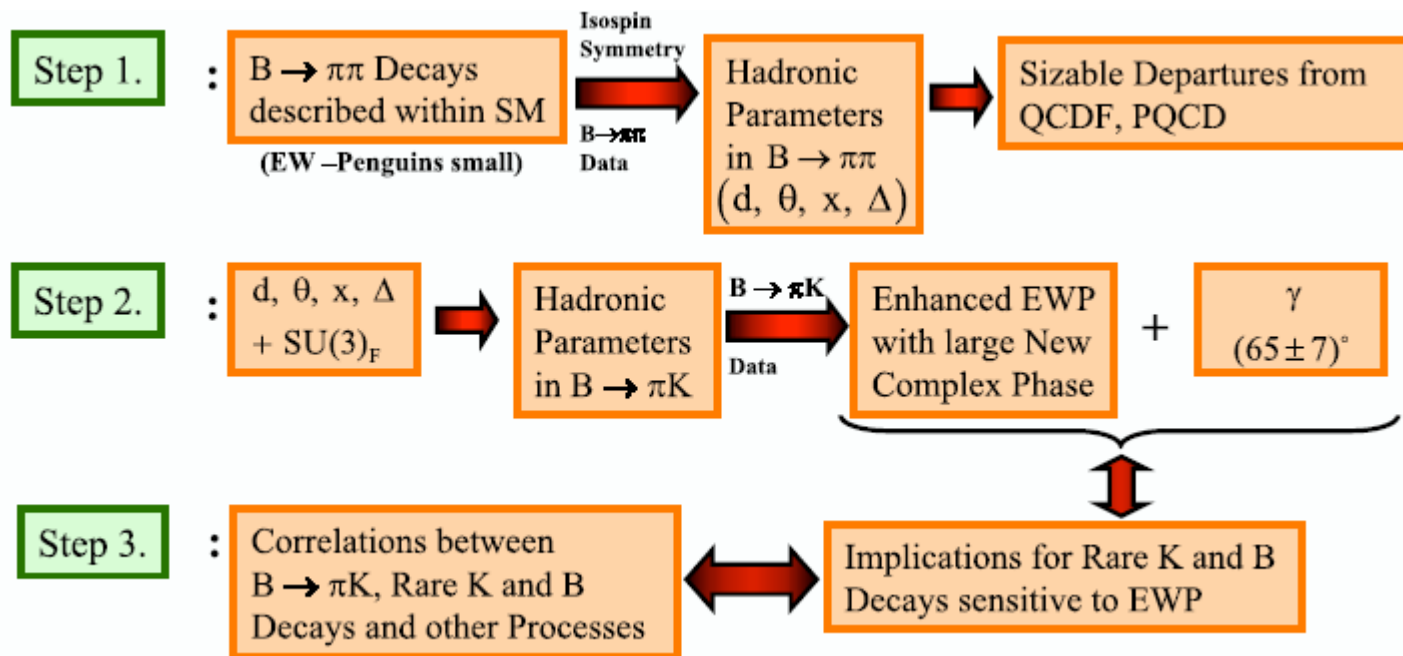
- during 90's: lots of sum rules/ratios/... to measure γ ; but: γ subleading, uncertain. not controlled
- now: input γ from global CKM fit, and study dynamics (mainly EWP sector, NP)
- is there a puzzle ? Buras et al, hep-ph/0309012

$$R_n = \frac{1 \text{ BR}(B^0 \rightarrow \pi^- K^+)}{2 \text{ BR}(B^0 \rightarrow \pi^0 K^0)} = 0.79 \pm 0.08 \quad \text{whereas } R_n > 1 \text{ in SM (??)}$$

Theory of $B \rightarrow \pi\pi$, $K\pi$ decays: series of short talks

■ Fleischer: [hep-ph/0312259](#), [hep-ph/0402112](#), [hep-ph/0410407](#)

🖥️ analysis strategy:



🖥️ $\pi\pi$ analysis shows

- agreement with SM (we knew this from isospin analysis already)
- sizable direct CPV in $\pi^0\pi^0$ expected
- large non-factorizable contributions (large “color-suppressed” amplitude)

strategy, ingredients to πK analysis, and results

- SU(3)-flavor
- neglect penguin annihilation and exchange topologies
- use $\pi\pi$ results as input and predict πK
- $A_{CP}(\pi^- K^+) = -0.13^{+0.10}_{-0.07}$ (in agreement with measurement)

study observables with sensitivity to EW penguins to search for NP

- R_c, R_n
- consider color-allowed EWP, neglect color-suppressed EWP

conclusions

- observables with tiny impact of EWP: agreement with SM
- observables with sizable impact of EWP: discrepancies with SM
- “puzzle” can be resolved with NP in EWP sector ($\rightarrow$ prediction of CPV effects in πK)

■ Charles ($B \rightarrow \pi K$ puzzle: how many pieces): hep-ph/0406184, and in preparation

🖥 point of critique: why should annihilation/exchange diagrams are negligible ?

- argument: power suppressed & $\sim f_B/m_B$ & small in QCDF (model)
- annihilation cannot be neglected in charm decays: $|A(B \rightarrow D_s K) / A(B \rightarrow DK)| \sim 10\%$
- $\text{BR}(K^+ K^-) / \text{BR}(\pi^+ \pi^-)$ weak estimator of annihilation ($< 30\%$ for amplitudes)

🖥 puzzles ?

- there is a $\pi\pi$ puzzle: why are “color-suppressed” terms so large ?
- there is no πK puzzle using $\text{SU}(2)$ [quadrilateral system not constraining enough]
- there seems to be a πK puzzle using $\text{SU}(3)$ when neglecting annihilation terms and $P_{\text{EW},C}$
- if one accepts that “color-suppression” has a problem, then $P_{\text{EW},C}$ could be large
- its inclusion is better than NP $\rightarrow$ no new parameters

🖥 side-remark (CKM information from CP and BR measurements, if $\text{BR}(K^+ K^-)=0$)

- $\pi^+ \pi^-$, $\pi^+ K^-$ measure α (and not γ) in strict $\text{SU}(3)$; UL on $\text{BR}(K^+ K^-)$ gives bound on $|\alpha - \alpha_{\text{eff}}|$
 - $\pi^0 \pi^0$, $\pi^0 K^0$ measure β (and not γ) in strict $\text{SU}(3)$
 - $\text{BR}(\pi^- K^+) C(\pi^- K^+) + \text{BR}(\pi^- \pi^+) C(\pi^- \pi^+) = 0 \quad (= 0.3 \pm 0.6)$
 - $\text{BR}(\pi^0 K^0) C(\pi^0 K^0) + \text{BR}(\pi^0 \pi^0) C(\pi^0 \pi^0) = 0 \quad (= 0.6 \pm 1.7)$
- } both satisfied in data
(note of course: these sum rules neglect annihilation!)

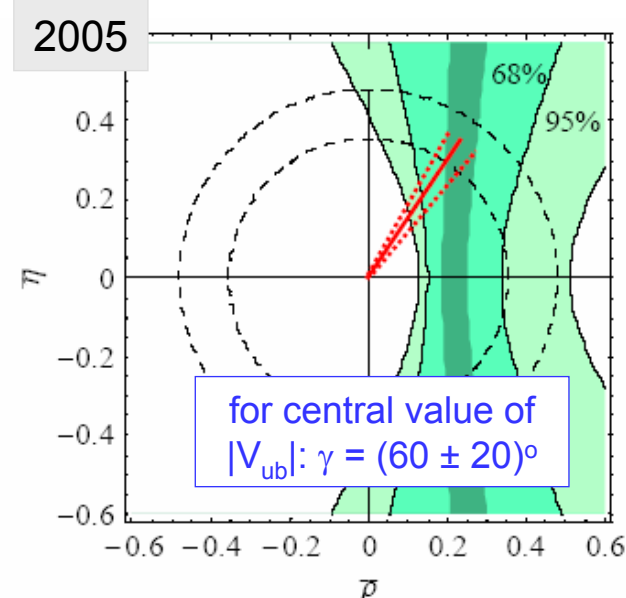
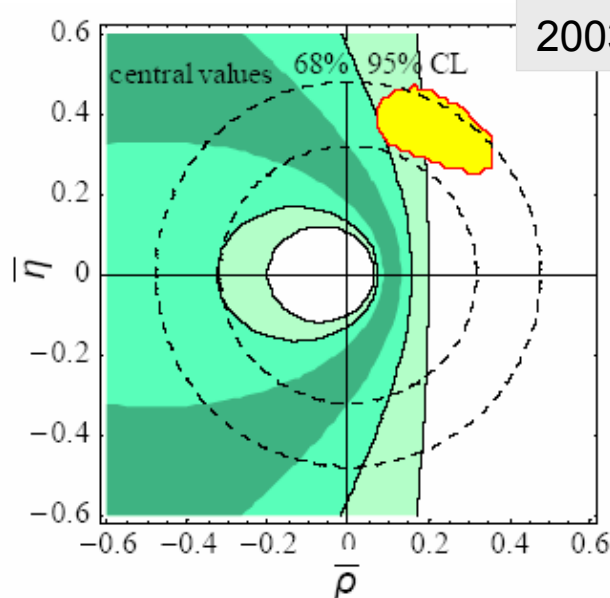
🖥 main result: without dynamical assumptions, derive significant constraint in ρ - η plane from combined $\pi\pi$, πK fit in strict $\text{SU}(3)$ limit. Marginal agreement with global CKM fit.

- Neubert (comments on $B \rightarrow \pi K$): using hep-ph/0308039

determination of γ

- get relevant input from data, up to SU(3) breaking corrections, which are calculable for $m_B \rightarrow \infty$
- residual uncertainties small: $\sim O(1/N_C \times m_s/m_b)$

$$R_* = \frac{1 \text{ BR}(B^+ \rightarrow \pi^+ K^0)}{2 \text{ BR}(B^+ \rightarrow \pi^0 K^+)} = 0.71 \pm 0.14 \text{ (2001); } 0.80 \pm 0.09 \text{ (2003); } 0.99 \pm 0.08 \text{ (2005)}$$



on the πK puzzle :

- defines yet another pair of ratios: R_{00} and R_L
- weak evidence ($< 3\sigma$) for new physics within QCDF approach to the πK puzzle

■ Yoshikawa (Large EW penguins):

hep-ph/0408090, hep-ph/0306147

🖥 ... it was a nice talk, but no particularly new results

🖥 general outline:

- diagrammatic approach (following Gronau-Hernandez-London-Rosner, eg, in hep-ph/9504327)
- full ansatz including all relevant EW penguins
- apply hierarchy assumptions
- fit to $B \rightarrow \pi K$ data

🖥 conclusions:

- $|P_{EW}/P| > \sim 0.2$ – but not enough to remove all discrepancies
- large strong phase between EWP and tree required
→ **or**: new physics phase, or large “color suppression”
- new physics phases must appear in direct CPV and $S(\pi^0 K^0)$

■ Also two brief discussion contributions from Sivestrini (charming penguins) and Lipkin (SU(3) relations between πK observables)

■ Feldman (Naively-, QCD- and non-factorizable effects):

hep-ph//0408188

Factorization

is really interested in understanding the dynamics

- naïve factorizable effects: $A_{M_1 M_2} \sim f_{M_1} F^{B \rightarrow M_2}$
- QCD-factorizable: $A_{M_1 M_2}^F \sim \alpha_S \cdot f(\phi_{M_i}, \phi_B, F^{B \rightarrow M_i})$
- non-factorizable effects (model-dependent)
 - power-suppressed: $A_{M_1 M_2}^{\text{NF}} \sim O(\Lambda / m_b)$
 - soft / endpoint sensitive effects: $A_{M_1 M_2}^{\text{NF}} \sim \alpha_S \ln(\Lambda / m_b)$

Typical QCD-improved $B \rightarrow \pi\pi$ analyses

- 7(-1) real parameters (isospin)
- assumptions about size of NF effects, eg, EW penguins are neglected
- ends up with 3-4 adjustable parameters (eg, X_A, X_H in BBNS, charm penguins, ...)
- present data show preference for large NF u -penguin compared to c -penguin

Long distance penguins and annihilation must be included when discussing NF effects

SU(3) and isospin violation

- $SU(3)_F$ breaking for NF amplitudes cannot be obtained from F ones
- can isospin-breaking corrections play a role in πK ? $\sim 5\%$?

 better control of power-suppressed effects is the most urgent theoretical issue

$B \rightarrow \pi\pi, K\pi$ decays: conclusions ?

- before becoming too quantitative, need updates of $\pi\pi, \pi K$ BRs (incl. radiative corrections)
- most phenomenological groups agree on where problems are/may be
- differences about what can be neglected
- certainly, within SU(2) there is no problem at all
- problems start within SU(3), and are also present in QCD-improved analyses
- control of power-suppressed terms is major theoretical challenge
- rather independent of the theoretical framework (QCDF, SCET, pQCD, ...)

more next week 😊